

1 Experimental measurement of cooling tower emissions  
2 using image processing of sensitive papers

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10 **Abstract**

11 Cooling tower emissions are harmful for several reasons such as air polluting,  
12 wetting, icing and solid particle deposition, but mainly due to human health  
13 hazards (i.e. Legionella disease). There are several methods for mea-  
14 suring drift drops. This paper is focussed on the sensitive paper technique,  
15 which is suitable in low drift scenarios and real conditions. The lack of an au-  
16 tomatic classification method motivated the development of a digital image  
17 process algorithm for the Sensitive Paper method. This paper presents a de-  
18 tailed description of this method, in which, drop-like elements are identified  
19 by means of the Canny blueedge detector combined with some morphologi-  
20 cal operations. Afterwards, the application of a J48 decision tree is proposed  
21 as one of the most relevant contributions. This classification method allows  
22 to discern between stains whose origin is a drop and stains whose origin is  
23 not a drop. The method is applied to a real case and results are presented  
24 in terms of drift and PM<sub>10</sub> emissions. This involves the calculation of  
25 the main features of the droplet distribution at cooling tower exit surface in

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26 terms of drop size distribution data, cumulative mass distribution curve and  
27 characteristic drop diameters. The Log-normal and the Rosin–Rammmler dis-  
28 tribution functions have been fitted to the experimental data bluecollected in  
29 the tests and it can be concluded that the first one is the most suitable for  
30 experimental data among the functions tested whereas the second one blueis  
31 less suitable. Realistic  $PM_{10}$  calculations blueincludes the measurement of  
32 drift emissions and Total Dissolved Solids as well as the size and number of  
33 drops. Results are compared to the method proposed by the blueU.S. En-  
34 vironmental Protection Agency assessing its overestimation. Drift emissions  
35 have found to be the 0.0517% of the recirculating water, which is over the  
36 limit of Spanish standards (0.05%).

37 *Keywords:*

38 Cooling tower emissions, Sensitive Paper, Canny edge detector, Log-normal  
39 distribution function

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## 40 **Nomenclature**

$A_p$	sensitive paper surface ( $m^2$ )
$A_T$	cooling tower exit surface ( $m^2$ )
$C_C$	Cunningham slip correction factor
$d_{0,1}$	10% spray proportion diameter, (m)
$d_{0,5}$	median diameter, (m)
$d_{0,9}$	90% spray proportion diameter, (m)
$d_{32}$	Sauter mean drop diameter, (m)
$d_d$	drop diameter, (m)
$d_p$	solid particle diameter, (m)

$d_s$	stain diameter, (m)
$\hat{d}$	Rosin–Rammler mean drop diameter, (m)
$D$	cooling tower drift
$E_c$	quadratic error
$f$	percent of solid mass emissions with $d_d \leq 10 \mu\text{m}$
$L$	characteristic dimension, (m)
$\dot{m}_d$	mass flow measured by the sensitive paper, ( $\text{kg s}^{-1} \text{ m}^{-2}$ )
$\dot{m}_s$	mass flow exiting the cooling tower, ( $\text{kg s}^{-1}$ )
$\dot{m}_w$	mass flow sprayed by the cooling tower, ( $\text{kg s}^{-1}$ )
$M_{Logn}$	Log-normal cumulative mass fraction
$M_{RR}$	Rosin–Rammler cumulative mass fraction
$n$	Rosin–Rammler shape factor
$n_p$	number of papers
$N$	number of drops
Stk	Stokes number
$t$	exposure time, (s)
$v$	relative velocity between the particle and the fluid stream, ( $\text{m s}^{-1}$ )
<i>Greek symbols</i>	
$\varepsilon$	collection efficiency
$\lambda$	Log-normal mean value
$\mu$	dynamic viscosity, ( $\text{kg m}^{-1} \text{ s}^{-1}$ )
$\rho$	density, ( $\text{kg m}^{-3}$ )
$\sigma$	Log-normal standard deviation
$\psi$	difference between calculated and experimental values
<i>Subscripts</i>	

$a$	fluid
TDS	total dissolved solids
$w$	particle

*Superscripts*

–	averaged value
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*Abbreviations*

EPA	Environmental Protection Agency
FN	False Negatives
FP	False Positives
PM <sub>10</sub>	Particulate Matter of 10 microns in diameter or smaller
RS	Relative Span
SF	Spread Factor
SP	Sensitive Paper
TN	True Negatives
TP	True Positives
TDS	Total Dissolved Solids

41 **1. Introduction**

42 Cooling systems have become essential in the daily bluelife. In fact, air  
 43 conditioning is directly responsible for the increase of the energy demand  
 44 of the blueservice industry. The increment of the installed power for appli-  
 45 cations of cooling systems has lead to an increase of the blueconsumption  
 46 peak. Depending on the application, different cooling technologies should be  
 47 applied in order to evacuate heat of a refrigeration cycle. Among all the ex-

48 istent solutions, two bluetypes can be distinguished: those which employ at-  
49 mospheric air as condensation element (air condensation systems) and those  
50 which use recirculation water to accomplish the same task (evaporative cool-  
51 ing systems). blue The main difference between water and air condensation  
52 systems is that the condensing temperature and pressure of the water cooled  
53 refrigerant systems is lower than the condensing temperature and pressure of  
54 the air cooled refrigerant systems. The fact that the condensing temperature  
55 and pressure of the water is lower means that, for the same cooling capacity,  
56 their energy consumption is also lower. Furthermore, an increase of CO<sub>2</sub>  
57 emissions to atmosphere is related to the lower energy efficiency of the air  
58 condensation systems.

59 The most bluewidely used water condensation systems is the cooling  
60 tower. The operation principle of cooling towers consists of an energy ex-  
61 change between water and air flows. During the process, the waterflow de-  
62 scends from the top of the tower to the tower basin. Meanwhile, a fan  
63 produces a vertical counterflow of the air in the opposite direction of blue-  
64 water. Water transfers heat to air producing the evaporation of a small part  
65 of the water and the cooling of the rest. This heat extracted from water is  
66 evacuated from the tower by means of the air flow.

67 In practice, it is possible that an extremely small part of water escapes  
68 from the tower as drops. The total quantity of drops taken away is known  
69 as drift. This drift means a water loss but also may produce several negative  
70 consequences: wetting, icing, salt deposition, and related problems such as  
71 damage to equipment or to vegetation (Talbot, 1967), as well as human  
72 health hazards.

73       When studying cooling tower emissions, it must be taken into account  
74 that drift is not pure water because it has the same composition of the  
75 recirculating water of the cooling tower. Therefore, drift will contain any  
76 impurities present in the recirculating water. This particulate matter will  
77 remain in the air and possibly deposit to the ground when the water of  
78 drops evaporates. AP-42 (EPA, 1995) describes a method to estimate  
79 the emission of particulate matter. This technique makes two assumptions:  
80 the total dissolved solids (TDS) are 11500 ppm and all dissolved solids con-  
81 tained in drift are PM<sub>10</sub>, that is to say, all diameters of solid particles are  
82 below 10  $\mu m$ . However, in the work of Reisman and Frisbie (2002), they  
83 considered that PM<sub>10</sub> is unrealistically modelled and thus proposed a  
84 more realistic method for estimating PM<sub>10</sub> emissions from cooling towers.  
85 This ambiguity led to consider the experimental measurement of the parti-  
86 cle matter emissions. This is tackled by measuring the TDS present in the  
87 recirculating water of the plant, the drift emitted and the size of the drops  
88 in the drift.

89       Among the problems related to cooling towers, Legionellosis is the most  
90 relevant. Legionellosis is caused by the Legionella, a bacterium whose habitat  
91 is the stagnant water. This bacterium proliferates specially in the presence  
92 of organic matter, temperatures between 20°C and 45°C, stagnant water or  
93 with low circulation and oxygen. The spread of this bacterium is probable  
94 due to aerosols in the system. In the case of cooling towers having  
95 insalubrious conditions (due to inappropriate maintenance), Legionella can  
96 be present in the water of the tower basin. If some drops escape from the  
97 tower (drift), Legionella will be spread. In fact, there is a risk of inhalation

98 depending on the size of the drops. In this way, it is necessary to develop  
99 a measurement technique that characterizes the quantity of drift as well  
100 the size of the drops. In Spain, the RD 865/2003 (BOE, 2003) establishes a  
101 maximum drift of 0.05% of the circulating water in the system. However, no  
102 method to measure this drift is mentioned.

103 In the literature, some methods to measure drift have been proposed (Lu-  
104 cas et al., 2012). Among these techniques, some countries have adopted one  
105 of them becoming a reference method. The method adopted by the British  
106 Standard BS 4485.2 (BS, 1988) and by the Japanese Industrial Standard  
107 JIS B 8609 (JIS, 1981) is the Thermal Balance Method. Other method is  
108 the one described in the Australian Standard AS 4180.1 (AS, 1994) named  
109 the Chloride Balance Method. The American Cooling Technology Insti-  
110 tute uses the Isokinetic Drift Test Code ATC 140 (CTI, 2011) and also refers  
111 to Sensitized Surface Methods. This methodology is described by Wilber  
112 and Vercauteren (1986).

113 Regarding the advantages of sensitive surface methods, the price is  
114 certainly the largest factor since sensitive papers are quite cheap compared  
115 to any device employed in drift measurements. Another strong point is the  
116 method capability of providing distributions of size and number of the drops  
117 collected. It presents, however, some disadvantages such as that it is im-  
118 possible to discern between drift and the condensed water produced by the  
119 mixture of the hot saturated flow exiting the tower and the cold and dry  
120 flow outside. It does not allow to discern between specific chemical tracers  
121 neither. Meanwhile, laser techniques are also capable of providing accurate  
122 drop distributions (size and number of drops) but besides the price, they are

123 not capable to perform field measures and are therefore most suitable for  
124 laboratory conditions.

125     Regarding the mentioned measuring methods, some comparative evalu-  
126 ation has been described in the literature. Roffman and Van Vleck (1974);  
127 Chen and Hanna (1978) presented a state of art blueview of measuring  
128 techniques for drift and deposition and a comparison between them. The  
129 most detailed comparison of methods was carried out by Golay et al. (1986).  
130 They described numerous techniques and devices to measure cooling tower  
131 drift emissions, diverse in terms of sophistication, basic principles of oper-  
132 ation and measurement capabilities. The results indicated that no single  
133 device is superior to the alternatives over the entire range of cases tested.  
134 Methods performing best under low water loading conditions utilize sensi-  
135 tive surface techniques. Methods performing best under high water loading  
136 conditions include the isokinetic mass sampling and chemical balance tech-  
137 niques. Additionally, Missimer et al. (1998) studied the relationship between  
138 Sensitive Paper and HGBIK drift measurements. The results showed similar  
139 results in both methods since the drift rate computed by the Sensitive Paper  
140 method was approximately 12% higher than the average rate estimated by  
141 the HGBIK method.

142     blueIn the current study, following the conclusions of Golay et al. (1986)  
143 the sensitive paper technique has been selected as the most suitable method  
144 to measure the drift bluefrom cooling towers with low levels of drift. This  
145 technique not only provides a quantitative drift value but also a qualita-  
146 tive information about droplet size distribution. Cizek and Novakova (2011)  
147 blueclassified the sensitive paper method as one of the most suitable for real

148 world conditions.

149 The information can be extracted from sensitive papers by means of dif-  
150 ferent techniques. First experiences to this method used a methodology to  
151 measure the number of drops captured by the sensitive papers. Particularly,  
152 in these techniques a human supervisor performed tasks of classification,  
153 evaluation and measurement. Later, some digital tools were employed. For  
154 example, Wilber and Vercauteren (1986) used the Digital Pen and there-  
155 fore the extraction of information was speeded up. In the recent years, the  
156 bluemannual methodology has made way to an automatic process due to the  
157 development of hardware and image processing techniques. In this work  
158 digital processing is applied in order to identify droplets in sensitive papers.

159 Regarding the detection of droplets on an image, some previous work has  
160 been performed. Bras et al. (2009) tried to model and validate liquid-liquid  
161 systems. They used a camera to capture an image of droplets on a fluid. In  
162 this case, the Hough Transform is used to detect drop-like structures and then  
163 recall-precision curves evaluate the accuracy of the droplets detection. Digital  
164 imaging processing was also used by Terblanche et al. (2009) to measure  
165 drops inside a cooling tower. Images are converted into white blobs over  
166 black background and the number of pixels included in each drop is counted  
167 in order to obtain the equivalent spherical diameter. This work aimed to  
168 determine the drop size distribution beneath different fills. As conclusion,  
169 they stated that the Rosin–Rammler distribution curve is not a suitable  
170 solution to fit to experimental data. Particularizing to the sensitive paper  
171 technique, Cruvinel et al. (1996) applied imaging processing to detect drops  
172 on sensitive papers using the Hough Transform and then drops are identified

173 by means of correlation with a patron. Hoffman and Hewitt (2005) extracted  
174 information from sensitive papers by means of three different methods and  
175 computed the correlation between them in terms of several definitions of the  
176 diameter that represents the drops distribution.

177 In this paper, digital processing to identify drops is tackled in three steps:  
178 detection, description and classification. Detection implies identification of  
179 drop-like elements. Then, these drops should be described and therefore two  
180 non-dimensional features are proposed. Finally, it is necessary to have  
181 an automatic classification method which is able to identify which stains come  
182 from real drops. In this work, some classification methods are tested in order  
183 to find the most suitable one for this purpose and the automation of this  
184 classification process is also presented.

185 The main objective of this paper is to describe the experimental setup  
186 and the techniques to measure the emissions of a cooling tower: drift and  
187  $PM_{10}$ . This study is applied to a real case and the results are discussed ac-  
188 cording to Spanish standards. The main features of the droplet distribution  
189 at cooling tower exit surface are presented in terms of drop size distribution  
190 data, cumulative mass distribution curve and characteristic drop diameters.  
191 Additionally, it is considered necessary to experimentally measure the par-  
192 ticle matter emissions. Finally, this work also aims to find a distribution  
193 function that fits suitably to the experimental data. The goodness of the fits  
194 is discussed through the quadratic error calculation.

## 195 **2. Method**

### 196 *2.1. Introduction*

197 Sensitive paper (SP) techniques are based on the collection of droplets  
198 taken away from a cooling tower by the air flow and collected by iner-  
199 tial impact thereof on a sensitive surface placed perpendicular to the flow.  
200 This paper is chemically treated (soaked in a solution of Potassium Fer-  
201 ricyanide [ $K_3Fe(CN)_6$ ], dried and dusted with Ferrous Ammonium Sulfate  
202 [ $Fe(NH_4)_2(SO_4)_2 \cdot 6H_2O$ ] powder). When a drop impacts on it, it creates  
203 a blue stain on the pale yellow background paper. The size and shape of  
204 the stain depends on the speed of impact and the original diameter of the  
205 drop. If the papers are exposed perpendicularly to the airflow, the stain will  
206 have a circular or nearly circular shape. The stain-drop size relationship can  
207 be known by calibrating the water-sensitive paper system by generating a  
208 known droplet's distribution with a generator of monodisperse drops in dif-  
209 ferent size ranges and rating them. The manufacturer provides a calibration  
210 curve where the spread factor (relation between the original diameter of the  
211 drop and the stain produced on the paper) is supplied. The sensitive paper  
212 with stains generated by drops of water, undergoes a process of scanning the  
213 image. First, the paper must be digitized in order to pass this information to  
214 the computer, which through an image processing program and analysis will  
215 be able to count, measure and classify the stains according to their size. This  
216 analysis leads to a droplet distribution by size based upon the calculation of  
217 the droplets diameters through the area covered by each stain. The proce-  
218 dure to experimentally determine the drift emitted by a cooling tower based  
219 on sensitive paper techniques involves to cover three main steps: carrying out

220 the tests, image processing and drift calculation. Each step is also divided in  
221 tasks; in the first step, number of papers and exposure time, carrying out the  
222 tests and storing the papers are carried out, in the second step, the scanning  
223 of the papers and the image processing using a computer are performed and  
224 finally, in the third step the cooling tower drift is calculated.

## 225 *2.2. Carrying out the tests*

226 Prior to performing the drift tests, the number and position of the pa-  
227 pers and exposure time shall be defined. The number of papers placed on  
228 cooling tower's exit surface will be selected with the purpose of gathering  
229 the maximum number of samples (papers) without influencing the measure.  
230 In rectangular cross-sectioned cooling towers rectangular papers and grid  
231 structure is recommended whereas in circular cross-sectioned cooling towers,  
232 circular papers forming concentric circles are the most proposed distribution.  
233 Moreover, the exposure time of the papers in the tests is the most important  
234 factor to be taken into account in the first step. Thus, a trial test to decide  
235 the best time has to be performed. The time will be considered as optimal  
236 when obtaining the maximum number of stains without the overlapping be-  
237 tween drops nor the edges paper becoming green due to the flow of moist  
238 air concentrated in that area. To establish the exposure time a compromise  
239 solution will be adopted in spite of the two conditions mentioned previously.  
240 Once the number of papers and exposure time have been set, tests are carried  
241 out and the papers are stored. The procedure to perform the tests and store  
242 the papers is detailed in section 3, where the SP method is applied to a real  
243 case.

244 *2.3. Image processing*

245 The digital processing of the papers is the second step of the method and  
246 covers from the scanning to the processing of the papers.

247 First, sensitive papers are digitized by means of a high resolution scanner.  
248 Then, all the stains present in the paper (coming or not from a real droplet)  
249 are detected, trying to extract as much information as possible from them.  
250 Next step is to describe these stains, and therefore some features should be  
251 selected so that drop-like stains are properly characterized. Finally, a classi-  
252 fier is employed to discern between “drop”, “no drop” and “multiple-drop”,  
253 based on the selected features. In the following, the process is described in  
254 detail.

255 *Stains detection.* This section explains how the digitized paper is processed in  
256 order to extract the maximum amount of information. The sensitive paper  
257 images are digitized in BMP format and have RGB information in their  
258 original form. However, for computing reasons, the work is performed with  
259 gray-scale images. As a consequence the image is separated into the R-, G-  
260 and B-channels and the R-channel is chosen as the most adequate. As it  
261 can be observed in figure 1, the R-channel presents more information than  
262 the B-channel and is more contrasted than the G-channel. As a result, the  
263 R-channel presents good defined stains in a well contrasted background and  
264 keeps all the necessary information.

265 Then, by means of the OpenCV library is used to extract all possible  
266 droplets from the paper. Particularly, drop-like stains are identified by means  
267 of the Canny edge detector, (Canny, 1986). This detection process is en-  
268 hanced by two morphological operations: dilate and erosion, furthermore

269 the contours are filled. All these operations eliminate noise and close the de-  
270 tected contours so that well-defined droplets are obtained. Figure 2 shows  
271 the droplets detected after Canny and the morphological operations.

272 Next step is to define features that describe the drop-like appearance of  
273 these stains and to train a classifier based on these features.

274 *Description.* Once the stains are detected, the next step is to describe them.  
275 For that reason, previous to classification, the selection of the features that  
276 characterize a drop are selected. These features are desirable to be non-  
277 dimensional so that this study can be extended to other cooling tower typolo-  
278 gies or other structural elements. Under these requirements, “Roundness”  
279 and “Hu Moments” were selected as classifying features. “Roundness” is pro-  
280 portional to the perimeter and area coefficient, whereas “Hu Moments” are  
281 dimensionless inertia moments based on the inertia moment of the detected  
282 drop.

283 Then, a training step is required in order to obtain the classifier based on  
284 the features and a training set. The training step as well as the classification  
285 step have been carried out by means of the WEKA software, (Hall et al.,  
286 2009). After a manual supervision, a training data set of 1037 samples was  
287 extracted from the papers. Moreover, different combinations of the classify-  
288 ing features testing “Roundness” and “Hu Moments” from 1 to 7 order have  
289 been considered. As a result of these tests, only “Roundness” and “1<sup>st</sup> Hu  
290 Moment” are significant features in the classification of the stains.

291 *Classification.* The stage of classification aims to obtain a reliable method  
292 which is able to identify different classes in the data obtained. Particularly,  
293 three different classes have been defined for classification of stains as shown in

294 figure 3. Stains coming from real drops belong to the “drop” class; those with  
295 a different origin are associated to the “no drop” class and, additionally, the  
296 case in which multiple drops overlap is also taken into account. This anomaly  
297 is tackled approximating those drops to a unique one, which is identify as  
298 the “multiple-drop” class.

299 The goodness of a classification method can be analyzed according to two  
300 criteria: a success rate measure and a confusion matrix. The success rate  
301 measures the percentage of correct classification cases, whereas the confusion  
302 matrix shows all the associations made. The general form of this confusion  
303 matrix is shown in table 1. The diagonal represents the true positives (TP),  
304 i.e., positive cases correctly classified and true negatives (TN), i.e., negative  
305 cases correctly classified. We consider that positive cases are “drop” and  
306 “multiple-drop” and the negative case is “no drop” class. Then, out of the  
307 diagonal there are the false positives (FP), i.e, negative cases classified as  
308 positive and false negatives (FN), i.e., positive cases classified as negative.  
309 In the ideal situation, would obtain a diagonal matrix. However, in practice  
310 values out of the diagonal are obtained. In this situation, it is desirable to  
311 obtain FP rather than FN, which means that some samples are incorrectly  
312 classified as drops. That is to say, the preference is not to lose information  
313 coming from real drops. In this work, two classification methods have been  
314 tested: Bayesian classifier and decision tree (J48). Table 2 shows the results  
315 obtained for each classification method. The results are presented in terms  
316 of success rate and confusion matrix, whose general form is explained in  
317 table 1. It can observed that J48 method obtains a higher success rate.  
318 Moreover, comparing the confusion matrix in both methods, J48 obtained

		Classified as		
		Drop	Multiple-drop	No drop
Actual class	Drop	TP	FP	FN
	Multiple-drop	FP	TP	FN
	No drop	FP	FP	TN

Table 1: Schematic description of the confusion matrix.

Type of classifier	Bayesian	Decision tree (J48)
Success rate (%)	92.7676	94.0212
Confusion matrix	$\begin{bmatrix} a & b & c \\ a & 775 & 8 & 0 \\ b & 12 & 187 & 0 \\ c & 17 & 38 & 0 \end{bmatrix}$	$\begin{bmatrix} a & b & c \\ a & 772 & 11 & 0 \\ b & 7 & 192 & 0 \\ c & 7 & 37 & 11 \end{bmatrix}$

Table 2: Success rate and confusion matrix for Bayesian and decision tree (J48) classifier. Subscript “a” stands for drop, “b” multiple-drop while “c” denotes no drop.

319 the highest success rate. In addition, J48 has a higher rate in false positives  
320 (FP) than in false negatives (FN), as it was preferable. This means that J48  
321 classifies wrongly stains as drops better than losing real drops. Given these  
322 results, it is considered that J48 is a suitable classifier using “Roundness”  
323 and “1<sup>st</sup> Hu Moment” as classifying features. We also consider that the non  
324 gaussianity of the classifying features justifies that the results obtained by the  
325 Bayesian method are less satisfactory. As a result of the drop detection and  
326 classification steps, a vector which includes the diameters of the stains that  
327 have been originated by drops is obtained (classified as “drop” or “multiple-  
328 drop”) detected in each sensitive paper.

329 *2.4. Data processing*

330 The image processing technique provides only the surface covered by the  
331 stains, but not the diameter of the drops which caused them. Thus the  
332 drop-stain relationship is employed. The calibration curve is supplied by the  
333 manufacturer where the spread factor (SF), defined in equation (1) is given.

$$\text{SF} = \frac{d_s}{d_d} \quad (1)$$

334 Tests have been performed using the Teejet model of hydrosensitive paper  
335 with dimensions of 52 x 76 mm, manufactured by Syngenta Crop. Protection  
336 AG., and distributed by Spraying Systems Co. The calibration curve is shown  
337 in figure 4. The spread factor alongside the stains vector provided in the  
338 previous step allow the calculation of the drop's diameter which has caused  
339 the stain.

340 Next, the collection efficiency is used to correct the error in such mea-  
341 surements where only the particles that impact on the collection surface are  
342 taken into account, not considering those particles which, because of their  
343 size or velocity, have been carried by the airflow.

344 A particle suspended in a fluid stream tends to move in a straight line  
345 because of its inertia. However, when the fluid meets an obstacle, the particle  
346 tends to move towards the obstacle and depending on factors such as particle  
347 velocity or particle diameter, it will end up hitting the obstacle or being  
348 deflected by the change of flow direction. Therefore, a parameter known as  
349 collection efficiency of the obstacle is defined. The inertial impactors, such  
350 as water-sensitive papers, have been studied extensively through theoretical  
351 and experimental studies (Ranz and Wong, 1952; Golovin and Putnam, 1962;  
352 May and Clifford, 1967).

353 The collection efficiency  $\varepsilon$ , is defined as the ratio between the number  
 354 of particles captured, compared to the total of particles injected into the  
 355 projected surface of the collector object, as shown in equation (2).

$$\varepsilon = \frac{N_{trapped}}{N_{injected}} \quad (2)$$

356 The Stokes number is the non dimensional parameter which appears after  
 357 performing a dimensional analysis to the problem of the collection efficiency  
 358 by inertial impact.

$$\text{Stk} = \frac{\rho_w d_d^2 v C_C}{18 \mu_a L} \quad (3)$$

359 The characteristic dimension,  $L$ , is usually determined as the projection  
 360 of the width of the object in the direction perpendicular to the flow. The  
 361 Cunningham correction factor should be applied to take into account that  
 362 the Stokes law ceases to be accurate when the particle size is similar to  
 363 the mean displacement of free gas molecules containing the particles. This  
 364 correction factor is close to unity, and hence negligible for particles in air at  
 365 normal temperature and pressure up to  $1 \mu\text{m}$  in diameter (Baron and Willeke,  
 366 2001). With smaller particles or low pressure conditions, the Cunningham  
 367 correction factor can be important. Figure 5 shows the collection efficiency  
 368 curve for ribbons, from the experimental data of May and Clifford (1967).

369 Having taken into account the spread factor and the collection efficiency,  
 370 drift can be calculated for each water-sensitive paper by equation (4).

$$\dot{m}_{d,i} = \frac{\rho_w \pi}{6 A_p t} \sum_{i=1}^N d_{d,i}^3 \varepsilon^{-1} \quad (4)$$

371 Where  $\varepsilon^{-1}$  is the associated collection efficiency for each  $d_{d,i}$ .

372 The mass flow of water that escapes through the outlet section of the  
373 tower, is calculated as:

$$\dot{m}_s = \frac{A_T}{n_p} \sum_{i=1}^{n_p} \dot{m}_{d,i} \quad (5)$$

374 Finally, drift is calculated as the ratio between the mass flow of water  
375 escaping from the tower  $\dot{m}_s$  and the total mass flow sprayed  $\dot{m}_w$ :

$$D = \frac{\dot{m}_s}{\dot{m}_w} \quad (6)$$

### 376 **3. Experimental apparatus**

377 In order to test the method, the amount of drift emitted by a bluecom-  
378 mercial cooling tower was experimentally calculated. The facility where the  
379 experiments were carried out, shown in figure 6, is assembled on the roof  
380 of a laboratory at the Universidad Miguel Hernández in the city of Elche,  
381 southeast of Spain. The main device of this test plant is a forced draft cool-  
382 ing tower with a cross-sectional area of 0.70 x 0.48 m<sup>2</sup>, a total height of  
383 2.597 m and a packing section that is 1.13 m high. The packing material  
384 consists of fiberglass vertical corrugated plates. Water pressure nozzles are  
385 used to distribute the water uniformly over the packing and the air is cir-  
386 culated counter-flow by an axial fan. The drift eliminator presents a zig-zag  
387 structure and consists of stainless steel plates separated at distance of 47  
388 mm. The fan's motor is equipped with a variable speed control, which allows  
389 the change of the air mass flow rate. Sprayed water mass flow rate can be  
390 changed manually by means of a balancing valve. Drift was calculated for  
391 nominal conditions (5200 l/h of mass flow rate and 50 Hz for the frequency  
392 switcher). A general-purpose data-acquisition system was set up to carry out

Magnitude	Day 1 (07/27/2011)	Day 2 (09/20/2011)
Water mass flow (kg/s)	1.424	1.431
Ambient temperature ( °C)	26.20	23.10
Output temperature ( °C)	23.56	20.16
Ambient relative humidity ( °C)	46.25	50.01
Output relative humidity (%)	99.23	97.38
Inlet water temperature ( °C)	20.94	18.88

Table 3: Averaged ambient and operating conditions registered during the tests.

393 the experimental tests. All data was monitored with an HP 34970A Data  
394 Acquisition Unit. Specific software was written and compiled for the system,  
395 supporting up to 36 inputs, with 16 bits A/D, 9600 bands transmission speed  
396 and programmable gain for individual channels.

397 Five sets of experiments were carried out in order to ensure the repeata-  
398 bility of the results. The first and second tests were performed during the  
399 morning of July the 27<sup>th</sup>, while the third, fourth and fifth took place on  
400 September the 20<sup>th</sup> (2011). The main parameters of the ambient and oper-  
401 ating conditions are shown in table 3.

402 To carry out the tests, the procedure defined in section 2.2 for the drift  
403 calculation is followed here. Once the cooling tower is operating under sta-  
404 tionary conditions (it requires at least half an hour in order to the drift  
405 eliminator to become saturated), the number of the papers was set to nine,  
406 placed at regions separated into three zones accordingly to the north-south  
407 axis of the tower. With the purpose of standardize the measures, an attach-  
408 ment for the cooling tower was built. This device, made of PVC, allows the

409 paper supports be fitted always in the same position and the tests not to be  
410 influenced by the wind. The setup described above (number and position of  
411 papers) has been taken as a reference for all the tests carried out. Regarding  
412 the interval, trial tests showed three seconds to be the optimal exposure time  
413 according to the compromise solutions criterion.

414 Having selected the exposure time, the real tests were performed follow-  
415 ing the sequence southern zone, central zone and northern one. Tests were  
416 performed using a rod where a PVC plate was used as a support for the  
417 papers. At the beginning of the test, the rod's shaft was to be held keeping  
418 the sensitive papers surface back to the flow at all times. In the start of the  
419 test the shaft of the rod has to be rotated  $180^\circ$  to place the paper surface  
420 perpendicular to the flow of moist air. After the selected time has passed, the  
421 rod is turned back so that the flow of moist air does not blow on the paper's  
422 yellow face, and it is immediately removed from the exit surface for droplets  
423 not to slide on it and not falling more drops on it. Figure 7 shows the cooling  
424 tower exit surface where the PVC support has been attached with the PVC  
425 plates used. Finally the papers were stored when they were completely dry.  
426 They were removed from the support taking great care not to damage nor  
427 contaminate them. And then, for the environmental conditions not to affect  
428 the papers, they were stored in vacuum bags. This solution is very practical,  
429 and also gives very good results because the papers remain unchanged the  
430 time it takes to begin the scanning process.

431 Regarding the scanning process, the equipment used is a professional  
432 photo scanner CanonScan 9950F model. It is a plain scanner with 4800 x  
433 9600 dots per inch of optical resolution. As for the scanning parameters, it

Test run	1	2	3	4	5
$\sum \dot{m}_{d,i}$ (kg s <sup>-1</sup> m <sup>-2</sup> )	0.017149	0.015745	0.020384	0.019225	0.017014
$\dot{m}_s$ (10 <sup>-4</sup> ) (kg s <sup>-1</sup> m <sup>-2</sup> )	7.0825	6.50263	8.41829	7.93957	7.02667
D (%)	0.049722	0.045651	0.058828	0.055483	0.049103

Table 4: Drift calculation results for the test runs 1 to 5.

434 was decided to scan the papers with the highest possible resolution of the  
435 scanner (4800 pixels per inch (5.291  $\mu\text{m}$  / pixel)) to lose as little information  
436 as possible. 24-bit true color has been selected for depth pixel, to get all the  
437 tonal changes in the paper. For processing these images with the computer,  
438 the BMP format was chosen. The scanning of the papers has been performed  
439 using the software provided by the scanner manufacturer. Finally the image  
440 process and drift calculation steps are performed.

#### 441 4. Results and discussion

442 blueThe results obtained from the bluefive sets of experiments carried  
443 out in the experimental facility are blue-described in this section. These are  
444 presented in terms of drift emissions and characteristic diameters, proposed  
445 functions to fit experimental drop size distributions and PM<sub>10</sub> emissions.

##### 446 4.1. Drift emissions and characteristic diameters

447 Table 4 shows drift emissions calculated according to equations (4), (5)  
448 and (6), while figure 8 depicts the drop distribution data for the set of ex-  
449 periments.

450 Paying attention to drift results, they show that the averaged value of the  
451 drift taken away from the tower is D=0.0517% with and standard deviation

452 of 0.00529%. This value is rather high compared to typical present-day man-  
453 ufacturers' guaranteed drift rates, which are on the order of 0.002% (EPA,  
454 1995). As the Spanish standards allow cooling towers to emit a maximum  
455 of the 0.05% of the circulating water, it can be said that the cooling tower  
456 operating under nominal conditions with the eliminator fitted is over the  
457 limit allowed. In that case, to ensure that the standards are upheld, it would  
458 be strongly recommended to replace the eliminator with another with higher  
459 efficiency or to change the geometry (number and shape of laths) to achieve  
460 better efficiencies.

461 For many purposes and in order to characterize the ensemble of drops  
462 exiting the tower, which contain drops of different sizes, a single number is  
463 required. Sometimes, the median diameter,  $d_{0,5}$ , (50% of the drops are larger  
464 and 50% are smaller than the median, in mass or volume terms) is employed.  
465 Moreover, according to Hoffman and Hewitt (2005), two additional droplet  
466 size parameters that are commonly used to describe more of the distribution  
467 than the median alone are the  $d_{0,1}$  and  $d_{0,9}$ . They describe the proportion of  
468 the spray volume (10% and 90%, respectively) contained in droplets of the  
469 specified size or less. Finally, the Relative Span (RS) is a measure of the  
470 width of the droplet spectra around the  $d_{0,5}$  defined in equation (7).

$$\text{RS} = \frac{d_{0,9} - d_{0,1}}{d_{0,5}} \quad (7)$$

471 In some cases, these diameters will suffice to describe the distribution, but  
472 because the drop surface area and volume are proportional to the square and  
473 cube of the diameter, respectively, a more complex description is required.

Test run	1	2	3	4	5
$d_{0,1}$ (mm)	0.0204	0.0218	0.0215	0.0206	0.0234
$d_{0,5}$ (mm)	0.0323	0.0326	0.0345	0.0344	0.0364
$d_{0,9}$ (mm)	0.0762	0.0779	0.0764	0.0746	0.0825
RS	1.7258	1.7202	1.5948	1.5710	1.6232
$d_{32}$ (mm)	0.0319	0.0325	0.0333	0.0327	0.0357

Table 5: Calculated values for  $d_{0,1}$ ,  $d_{0,5}$ ,  $d_{0,9}$ , RS and  $d_{32}$  for the test runs 1 to 5.

474 A general mean diameter can be defined by

$$d_{pq} = \left[ \frac{\sum_{i=1}^N d_{d,i}^p \varepsilon_i^{-1}}{\sum_{i=1}^N d_{d,i}^q \varepsilon_i^{-1}} \right]^{\left(\frac{1}{p-q}\right)} \quad (8)$$

475 According to Terblanche et al. (2009), the Sauter mean diameter represents  
476 mean diameter with the same ratio of volume to surface area as the entire  
477 ensemble. It corresponds to values of  $p = 3$  and  $q = 2$  in equation (8). The  
478 Sauter mean diameter ( $d_{32}$ ) is probably the most commonly used mean as  
479 it characterizes a number of important processes. Chin and Lefebvre (1985)  
480 suggested that it is the best measure of the fineness of sprays.

481 Results of  $d_{0,1}$ ,  $d_{0,5}$ ,  $d_{0,9}$ , RS and the  $d_{32}$  are presented in table 5. As it can  
482 be observed, the sequence of diameters attending to its size is, as expected,  
483  $d_{0,9}$ ,  $d_{0,5}$ ,  $d_{32}$  and  $d_{0,1}$  (Williams, 1990). Since the standard deviation to mean  
484 value ratio of all of the parameters is lower than 5%, repeatability can be  
485 ensured.

#### 486 4.2. Drop size distributions fits

487 It is important to have experimental data that can be fitted to a  
488 theoretical model in order to best define a numerical model for predicting

489 the dispersion and deposition of cooling tower drift. In the literature, some  
 490 numerical models are available that have been evaluated using experimental  
 491 data from several sources. Meroney (2006) and Lucas et al. (2010) used  
 492 the experimental data taken from the bluestudy of Policastro et al. (1981)  
 493 to validate their numerical dispersion and deposition results. They both  
 494 employed the Rosin–Rammler function to fit the experimental data of the  
 495 drops blueemitted from the cooling tower. However, according to Terblanche  
 496 et al. (2009), fitting the Rosin–Rammler functions to experimental data does  
 497 not provide consistent curve fits and blueshould be avoided. Nonetheless,  
 498 they propose no bluealternative function.

499 In order to assess the conclusions reached by Terblanche et al. (2009)  
 500 regarding the Rosin–Rammler function, and aiming to determine the most  
 501 suitable function for fitting droplet distributions, the Rosin–Rammler, the  
 502 Modified Rosin–Rammler and the Log-normal distribution functions have  
 503 been fitted to the experimental data and the goodness of the fits has been  
 504 blueetermined through the quadratic error calculation.

505 A cumulative mass distribution is a distribution curve which gives mea-  
 506 sured cumulative mass fraction data as a function of drop diameters. blueThe  
 507 cumulative mass fraction at a certain drop diameter is defined as the drop  
 508 mass fraction of which the drop diameters are bluesmaller than that spe-  
 509 cific diameter. The Rosin–Rammler function is an empirical relation used to  
 510 correlate measured cumulative mass distribution data, expressed as

$$blueM_{RR} = 1 - e^{-\left(\frac{d}{\hat{d}}\right)^n} \quad (9)$$

511 where the Rosin–Rammler mean drop diameter,  $\hat{d}$ , is obtained from the mea-  
 512 sured cumulative mass distribution at the diameter where the cumulative

513 mass distribution is  $1 - e^{-1}$  while the shape factor,  $n$ , can be determined  
 514 by an average of equation (10) for each drop diameter interval.

$$bluen = \frac{\ln(\ln M_{RR})}{\ln \frac{d}{\hat{d}}} \quad (10)$$

515 As mentioned above, the Rosin-Rammler distribution has been found by  
 516 others to not produce the best agreement with experiment data and other  
 517 distributions are preferable. Here, the Modified Rosin-Rammler function is  
 518 proposed, where the set of parameters  $\hat{d}$  and  $n$ , have been selected in order to  
 519 minimize the error between calculated and experimental results. Finally the  
 520 Log-normal function, which according to Linmpert et al. (2001) is suitable  
 521 for size distributions of aerosols, can be expressed as

$$M_{Logn} = \frac{1}{2} \left[ 1 + \operatorname{erf} \left( \frac{\ln d - \lambda}{\sqrt{2\sigma^2}} \right) \right] \quad (11)$$

522 where  $\lambda$  and  $\sigma$  are the mean and standard deviation, respectively, of the  
 523 variable's natural logarithm and erf is the error function defined as

$$\operatorname{erf}(x) = \frac{2}{\sqrt{\pi}} \int_0^x e^{-t^2} dt \quad (12)$$

524 Figure 9 depicts the drop size distribution data and the cumulative mass  
 525 distribution curves for the tests carried out.

526 The goodness of the fits can be shown using the quadratic error calcu-  
 527 lation,  $E_c$ . The magnitude, defined in equation (13), measures the ratio  
 528 of the square difference between calculated and experimental values ( $\psi$ ) to  
 529 the number of drops ( $N$ ).

$$E_c = \frac{\sum_{i=1}^N \psi_i^2}{N} \quad (13)$$

Test run		1	2	3	4	5
Rosin–Rammler	$\hat{d}$ (mm)	0.0381	0.0382	0.0402	0.0401	0.0427
	$n$	2.1833	2.2064	2.2570	2.2032	2.2816
	$E_c$	0.0040	0.0039	0.0034	0.0035	0.0039
Modified Rosin–Rammler	$\hat{d}$ (mm)	0.0513	0.0518	0.0520	0.0513	0.0556
	$n$	1.2694	1.3273	1.3660	1.3470	1.3779
	$E_c$	0.0035	0.0038	0.0029	0.0025	0.0035
Log-normal	$\lambda$	-3.3015	-3.2806	-3.2689	-3.2840	-3.2009
	$\sigma$	0.5971	0.5776	0.5662	0.5720	0.5647
	$E_c$	0.0011	0.0013	0.0010	0.0009	0.0010

Table 6: Fitting parameters  $\hat{d}$  and  $n$  for Rosin–Rammler and Modified Rosin–Rammler functions and  $\lambda$  and  $\sigma$  for Log-normal function; Quadratic error results.

530 The fitting parameters  $\hat{d}$  and  $n$  for both Rosin–Rammler functions,  $\lambda$  and  $\sigma$   
531 for the Log-normal and the values of the  $E_c$  for the three distributions, are  
532 presented in table 6.

533 Results show that the maximum error blueoccurs for the Rosin–Rammler  
534 function followed by the modified Rosin–Rammler and the Log-normal func-  
535 tion. This fact corroborates the conclusions reached by Terblanche et al.  
536 (2009), bluewho advised to avoid the Rosin–Rammler function. In the present  
537 case this functions bluehas the maximum error between calculated and ex-  
538 perimental data for all of the tests performed. Despite blueethe fact that the  
539 function is able to predict correctly the beginning and the centre of the curve,  
540 it ceases to be accurate for the blueasymptotic behaviour at the end of the  
541 curve. blueThe Modified Rosin-Rammler distribution was proposed in order

542 to correct the problem. In this function, the mean and shape factors ( $\hat{d}$  and  
543  $n$ ) are calculated blueby minimizing the error criterion. However, despite  
544 bluethe fact that this function bluebetter fits the experimental data than the  
545 Rosin–Rammmler function, specially at the asymptote, it fails at the centre  
546 of the curve. Meanwhile, the Log-normal bluehas the minimum quadratic  
547 error for all the tests performed and predicts very well blueat all parts of the  
548 curve.

#### 549 *4.3. PM<sub>10</sub> emissions*

550 blueThe calculations of PM<sub>10</sub> emissions are discussed in this subsection.  
551 The EPA (1995) AP-42 report states that the particulate matter constituent  
552 of the drift droplets may be classified as an emission because the direct  
553 contact between the cooling water and the air passing through the tower.  
554 blueA conservative method is proposed to calculate the PM<sub>10</sub> emission factor,  
555 which can be estimated, (a), by multiplying the total liquid drift factor by  
556 the total dissolved solids (TDS) fraction in the circulating water and (b),  
557 by assuming that, once the water evaporates, all remaining solid particles  
558 are within the PM<sub>10</sub> size range. blueThe values provided by AP-42 (EPA,  
559 1995) for drift emissions and TDS in wet mechanical cooling towers are 0.02%  
560 and 11500 ppm respectively. However, Reisman and Frisbie (2002) proposed  
561 bluean alternate realistic method to calculate the PM<sub>10</sub> emissions based upon  
562 the fact that not all the solids which escape through the tower are particles.  
563 They concluded that the AP-42 method (EPA, 1995) does not account for  
564 the droplet size distribution of the drift exiting the tower and hence this is  
565 a critical factor, as more than 85% of the mass of particulate in the drift  
566 from most cooling towers will result in solid particles larger than blue10  $\mu\text{m}$

567 once the water has evaporated. Particles larger than blue10  $\mu\text{m}$  are no longer  
568 a regulated air pollutant, because their impact on human health has been  
569 shown to be insignificant.

570 The procedure to calculate  $\text{PM}_{10}$  emissions according to Reisman and  
571 Frisbie (2002) is shown bluebelow.

$$\text{PM}_{10} = \text{PM } f = \dot{m}_s \text{ TDS } f \quad (14)$$

572

$$d_p = d_d \left( \text{TDS} \frac{\rho_w}{\rho_{\text{TDS}}} \right)^{\frac{1}{3}} \quad (15)$$

573 blueFor the present study,  $\text{PM}_{10}$  emissions have been calculated using the  
574 EPA (1995) AP-42 method, for the water mass flow rates shown in table 3  
575 and the above given values of 11500 ppm for the TDS and 0.02% for drift  
576 emissions. blueAlso emissions have been calculated blueusing the Reisman  
577 and Frisbie (2002) method for the drift emissions presented in table 4 and a  
578 water density to TDS density ratio equal to 0.461. The TDS content has been  
579 estimated by blueusing the TDS observations for the make-up water (462  
580 ppm) and multiplying them by blue3 cooling tower cycles of concentration  
581 (it usually ranges from 3 to 7 in the majority of cooling towers), for a total  
582 of TDS=1386 ppm in mass. The results of the bluecompararison of methods  
583 are shown in table 7.

584 As expected, results blueshow that the AP-42 method overestimates the  
585  $\text{PM}_{10}$  emitted by the tower. The difference is about one order of magnitude.  
586 Results for the Reisman and Frisbie (2002) method show slightly differences  
587 between PM and  $\text{PM}_{10}$  emissions because blueethe quantity of TDS present in  
588 the water is low. Hence, once blueevaporated from the water, most of solid  
589 particles have diameters smaller than 10  $\mu\text{m}$ . Thus the percent of solid mass

Test run	1	2	3	4	5
PM <sub>10</sub> (10 <sup>-6</sup> ) (kg s <sup>-1</sup> ) <sup>a</sup>	3.275	3.275	3.291	3.291	3.291
PM (10 <sup>-6</sup> )(kg s <sup>-1</sup> )	0.982	0.901	1.167	1.100	0.974
<i>f</i> (%)	94.65	94.51	95.05	95.36	94.63
PM <sub>10</sub> (10 <sup>-6</sup> ) (kg s <sup>-1</sup> ) <sup>b</sup>	0.929	0.852	1.109	1.049	0.922

Table 7: PM, *f* and PM<sub>10</sub> blueemissions calculations for the tests performed in the facility described in section 3. a) Calculated according to EPA (1995) AP-42 method; b) Calculated according to the Reisman and Frisbie (2002) method.

590 emissions bluewhose diameter is equal to, or smaller than 10  $\mu\text{m}$ , *f*, is close  
591 to 100 %. blueHowever a difference would be found if the amount of TDS  
592 increases.

593 blueEven if the TDS content of the water increases, a scenario where PM<sub>10</sub>  
594 emissions calculated according to EPA (1995) AP-42 method would be lower  
595 than PM<sub>10</sub> emissions calculated according to the Reisman and Frisbie (2002)  
596 method seems unlikely. The reason is that, despite the fact that the PM to  
597 TDS ratio increases in a straight line, the PM<sub>10</sub> to TDS ratio will begin to  
598 decline at some point because of the decreasing of *f*. At higher TDS, the  
599 drift drops will contain more solids, and so, even after evaporation, they will  
600 result in larger solid particles for any given initial droplet size. However,  
601 the difference between the EPA (1995) AP-42 and the Reisman and Frisbie  
602 (2002) PM<sub>10</sub> emissions could have increased if a high-efficiency eliminator  
603 would have been used in our test experiments presented.

604 In conclusion it can be said that in the case presented in this paper  
605 the overestimation PM<sub>10</sub> blueemissions by the method described in blueAP-  
606 42 (EPA, 1995) was found. blueIt is therefore recommended that a real

607 calculation be performed of the  $PM_{10}$  emissions because factors such as the  
608 drift rate or the TDS value are subject to change depending on the facility  
609 where the drift is measured. Thus, the necessity of measuring not only TDS  
610 and drift but the distribution of diameters (size and number) is highlighted.  
611 In this sense the sensitive paper has proven to be suitable for the purpose.

## 612 5. Conclusions

613 This paper aims to describe the experimental setup and the techniques to  
614 measure the emissions of a cooling tower using the sensitive paper method.  
615 The digital image process developed in order to measure the emissions is  
616 described. For that purpose sensitive papers are scanned after perform-  
617 ing a drift test to obtain a digital image. Drop-like elements are identified  
618 by means of the Canny edge detector enhanced by some morphological oper-  
619 ations (dilate, erosion and filling). To identify those stains whose origin  
620 is a drop, a classification method based upon two non-dimensional char-  
621 acteristics of the droplets (roundness and the 1<sup>st</sup> Hu Moment) is proposed.  
622 This classification method, the J48 tree, was selected after it was found  
623 to achieve the highest success rate. It is also capable of dealing with anoma-  
624 lies such as overlapping drops, classifying them as a multiple drops. This  
625 classification method has proven to be one of the most relevant contributions  
626 of this work.

627 The application of the method to a real case has yielded estimates  
628 of emissions of droplets and distribution data curves and  $PM_{10}$  emis-  
629 sions, and can be summarized as follows. Drift emissions of the tower  
630 operating under nominal conditions are  $D=0.0517\%$ . This drift emis-

631 sion measurement is over the Spanish standard limits (0.05%). Therefore  
632 replacing the drift eliminator for another with higher efficiency would be ad-  
633 visible, blueespecially because today technologies can guarantee lower drift  
634 rates. The drop size distribution calculated in terms of characteristic di-  
635 ameters ensures the repeatability of the results even measured in different  
636 ambient conditions. The influence of operating conditions shall be studied  
637 in future works.

638 blueCorrelations for the cumulative mass distribution have been derived  
639 from the observations and three functions have been fitted to them. The  
640 goodness of the fits has been blueestimated through the quadratic error cal-  
641 culation. blueThe Log-normal distribution function has proven to yield the  
642 best fits, ( $\bar{E}_c=0.00106$ ) better than bluethe Modified Rosin–Rammler func-  
643 tion ( $\bar{E}_c=0.00324$ ) blueand the Rosin–Rammler ( $\bar{E}_c=0.00374$ ).

644 bluePM<sub>10</sub> emissions have also been calculated according to the AP-42  
645 (EPA, 1995) and Reisman and Frisbie (2002) methods. blueThe overestima-  
646 tion of the PM<sub>10</sub> emissions calculation by the EPA method is assessed. It  
647 is strongly recommended that a separate calculation be performed for each  
648 cooling tower because factors such as drift rate and  $f$  can be modified de-  
649 pending on the drift eliminator blueinstalled in the tower or the amount of  
650 TDS present in the water. As this calculation requires quantitative (amount  
651 of drift) and qualitative (size and number of drops) information, sensitive  
652 surface methods are suggested to measure PM<sub>10</sub> in real facilities. blueThese  
653 statements are mainly based on analysis of observations from the research  
654 apparatus presented in the section 3 and, despite the fact that the cooling  
655 tower is operating in the typical operating cooling tower conditions, there is

656 a future need to test the sampling methods and the drop size distribution  
657 formulas with independent data. blue

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740 **7. Captions for figures**

741 Figure 1: (a) Original image, (b) R-channel, (c) G- channel and (d) B-  
742 channel.

743

744 Figure 2: (a) Original image and (b) processed image.

745

746 Figure 3: Data types for the stains detected. a) “No Drop”, b) “Drop”  
747 and c) “Multiple Drop”.

748

749 Figure 4: Spread factor curve for Teejet 52 x 76 mm paper.

750

751 Figure 5: Experimental impaction efficiency of ribbons provided by May  
752 and Clifford (1967) and schematic arrangement of particle deposition on sen-  
753 sitive papers.

754

755 Figure 6: Arrangement of the pilot test facility assembled at Universidad  
756 Miguel Hernández, Elche (Spain).

757

758 Figure 7: PVC attachment and plates used in the drift tests.

759

760 Figure 8: Experimental drop size distribution data.

761

762 Figure 9: Experimental cumulative drop mass distribution, Rosin–Rammler  
763 distribution, Modified Rosin–Rammler distribution and Log-normal distribu-  
764 tion curves.

765

766 **Figures**

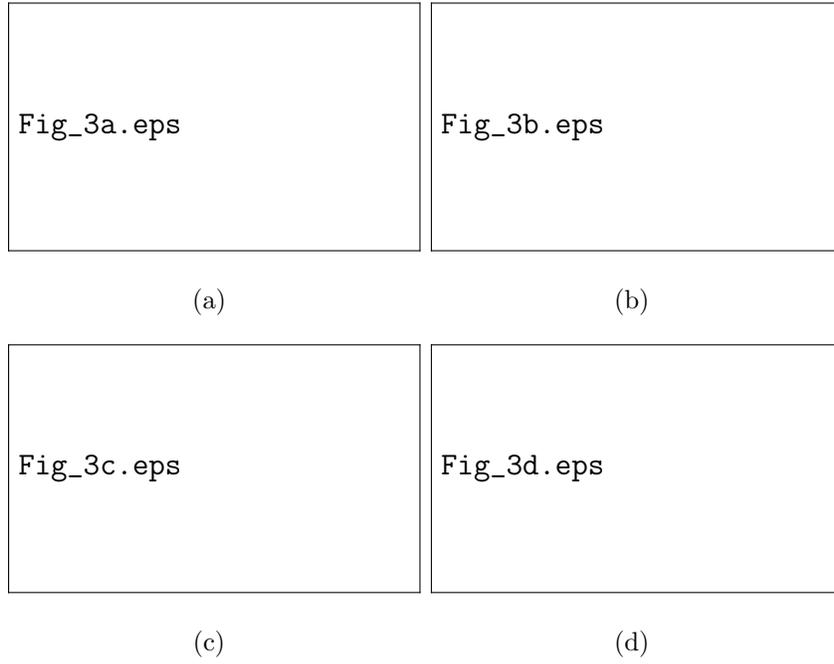
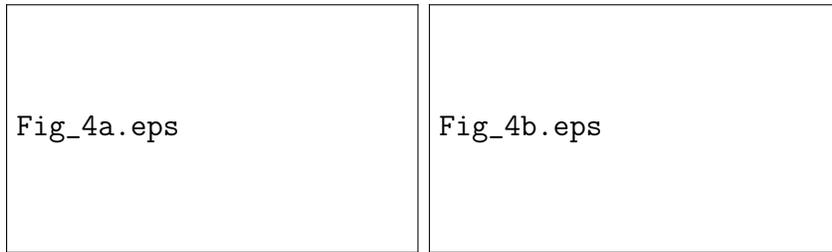


Figure 1: (a) Original image, (b) R-channel, (c) G- channel and (d) B-channel.



(a)

(b)

Figure 2: (a) Original image and (b) processed image.

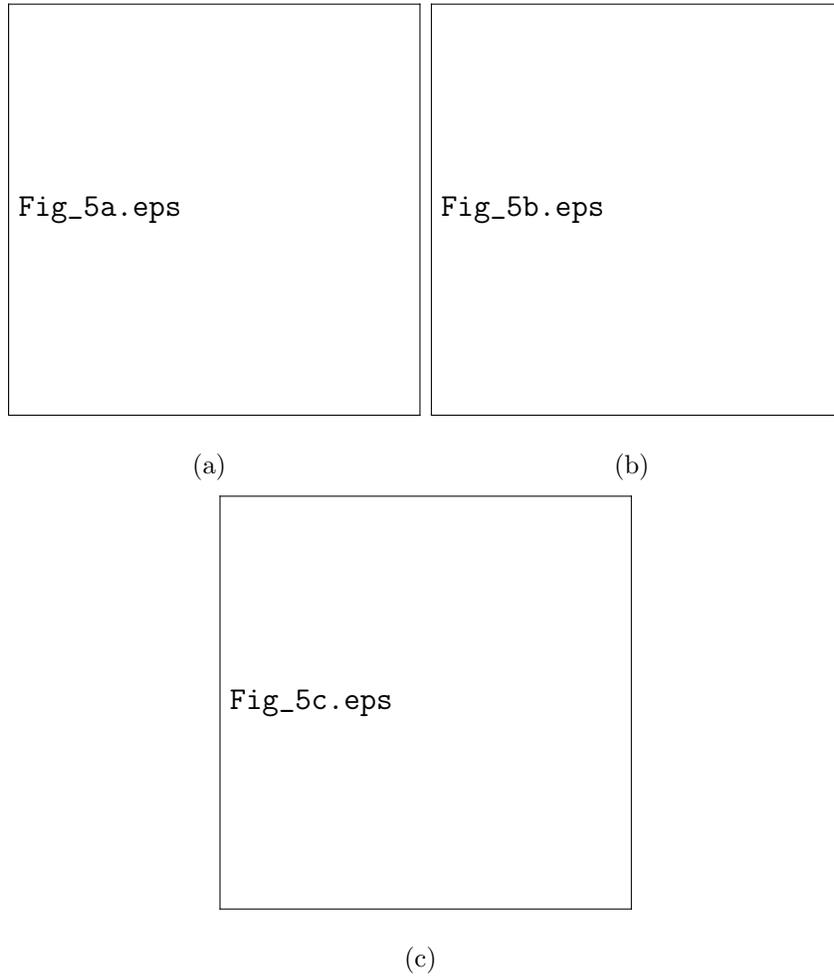


Figure 3: Data types for the stains detected. a) “No Drop”, b) “Drop” and c) “Multiple Drop”.



Figure 4: Spread factor curve for Teejet 52 x 76 mm paper.

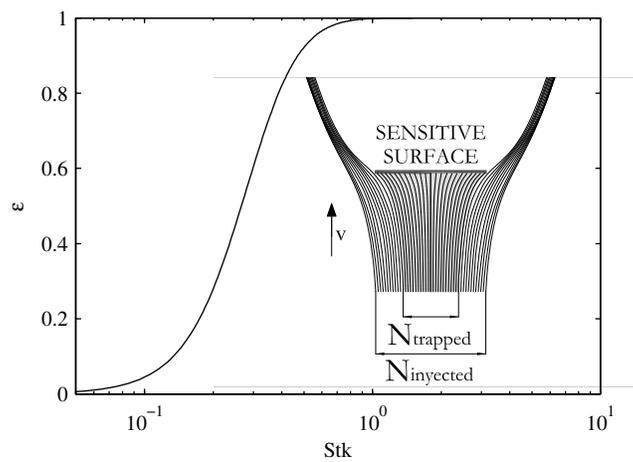


Figure 5: Experimental impaction efficiency of ribbons provided by May and Clifford (1967) and schematic arrangement of particle deposition on sensitive papers.

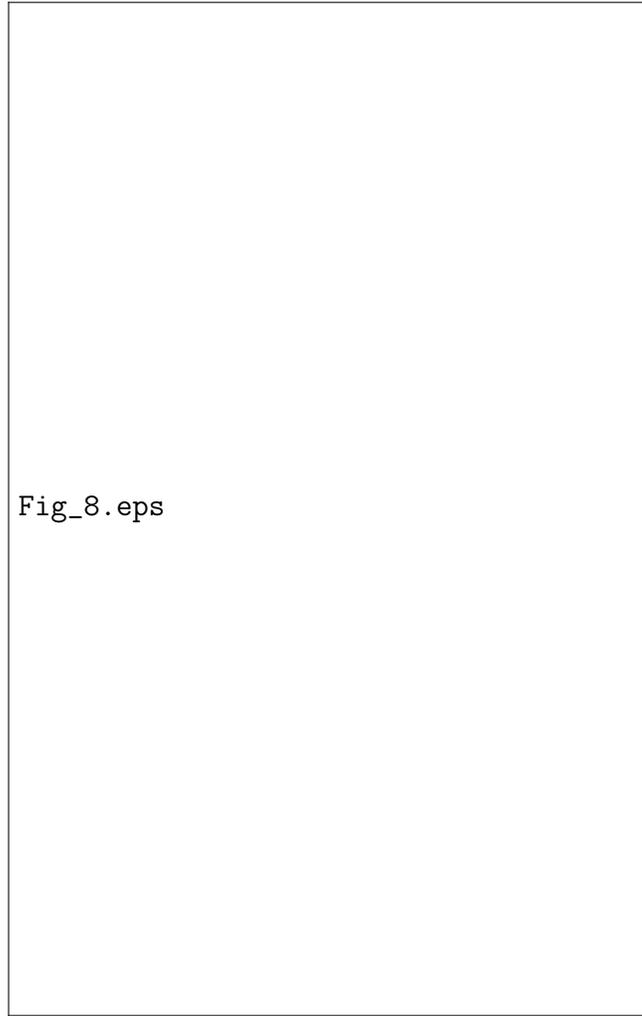


Figure 6: Arrangement of the pilot test facility assembled at Universidad Miguel Hernández, Elche (Spain).

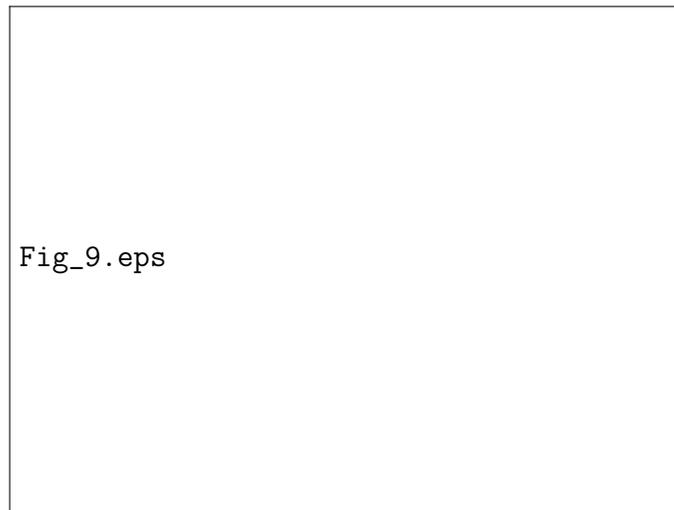
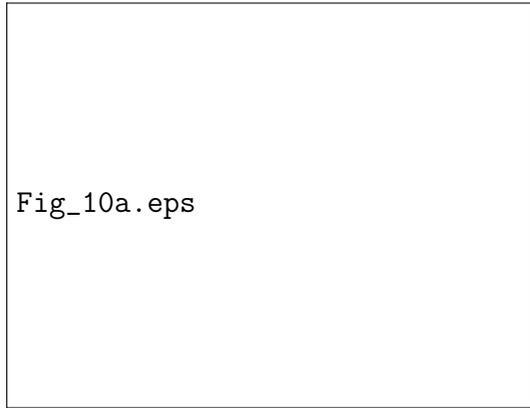


Figure 7: PVC attachment and plates used in the drift tests.



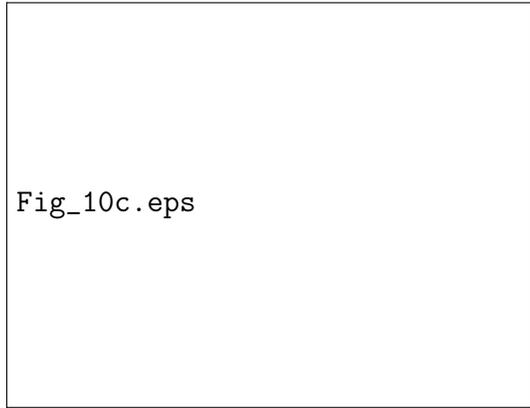
Fig\_10a.eps

(a) Test run number 1



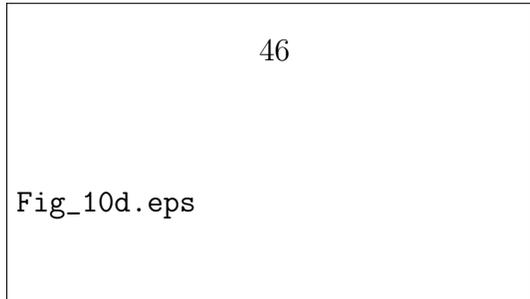
Fig\_10b.eps

(b) Test run number 2



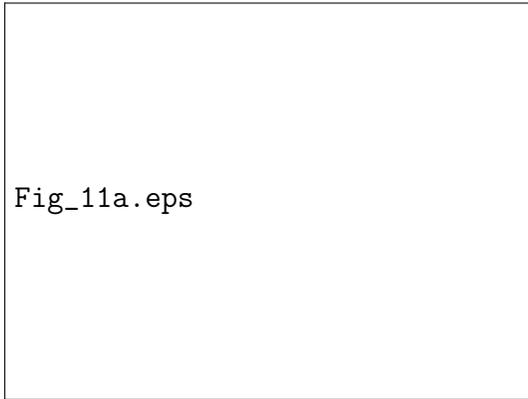
Fig\_10c.eps

(c) Test run number 3



46

Fig\_10d.eps



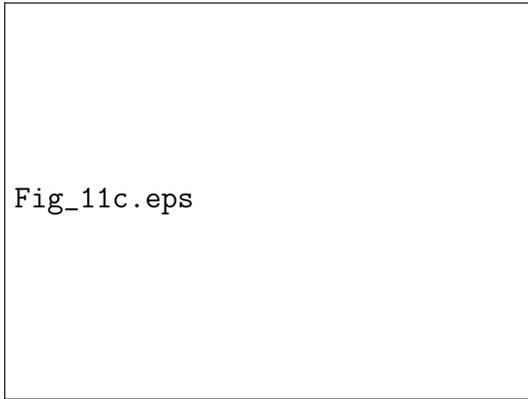
Fig\_11a.eps

(a) Test run number 1



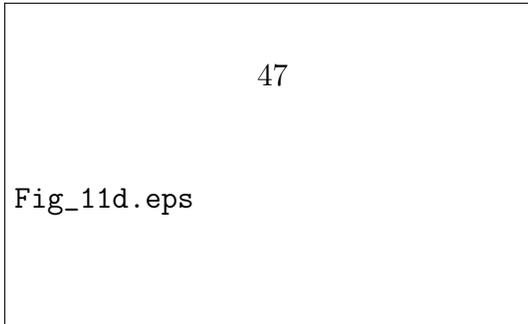
Fig\_11b.eps

(b) Test run number 2



Fig\_11c.eps

(c) Test run number 3



47

Fig\_11d.eps