



# ICINCO 2011

8<sup>th</sup> International Conference on Informatics in Control, Automation and Robotics

## Proceedings

Volume 2

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28 - 31 July, 2011

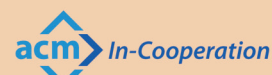
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# BUILDING VISUAL MAPS WITH A SINGLE OMNIDIRECTIONAL CAMERA

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**Keywords:** SLAM, Visual SLAM, Omni-directional images.

**Abstract:** This paper describes an approach to the Simultaneous Localization and Mapping (SLAM) problem using a single omnidirectional camera. We consider that the robot is equipped with a catadioptric sensor and is able to extract interest points from the images. In the approach, the map is represented by a set of omnidirectional images and their positions. Each omnidirectional image has a set of interest points and visual descriptors associated to it. When the robot captures an omnidirectional image it extracts interest points and finds correspondences with the omnidirectional images stored in the map. If a sufficient number of points are matched, a translation and rotation can be computed between the images, thus allowing the localization of the robot with respect to the images in the map. Typically, visual SLAM approaches concentrate on the estimation of a set of visual landmarks, each one defined by a 3D position and a visual descriptor. In contrast with these approaches, the solution presented here simplifies the computation of the map and allows for a compact representation of the environment. We present results obtained in a simulated environment that validate the SLAM approach. In addition, we present results obtained using real data that demonstrate the validity of the proposed solution.

## 1 INTRODUCTION

Many applications in the field of mobile robots require the existence of a map that represents the environment. Thus, the construction of a map is a key ability for an autonomous vehicle. In order to build the map the robot must explore the environment to gather data and compute a coherent map. Commonly, the pose of the robot during the exploration process is unknown, leading to the problem of Simultaneous Localization and Mapping (SLAM). In these situations, the robot needs to build a map incrementally, while, simultaneously, computes its location inside the map.

To date, due to their precision, laser range sensors have been used to build maps (Stachniss et al., 2004; Montemerlo et al., 2002). Typically, these applications use directly the laser measurements to build 2D occupancy grid maps (Stachniss et al., 2004), or they extract features from the laser measurements (Montemerlo et al., 2002) to build 2D landmark-based maps.

During the last years, a great number of approaches propose the utilisation of cameras as the main sensor in SLAM. These applications are usually denoted as visual SLAM. Compared to laser ranging systems, cameras are typically less expensive and pro-

vide a huge quantity of 3D information (projected on a 2D image), whereas typical laser range systems allow to collect distance measurements only on a 2D plane. However, vision sensors are generally less precise than laser sensors and require a significant computational effort in order to find usable information for the SLAM process.

Different approaches to SLAM using vision sensors have been classified under the name of visual SLAM. In these group, we can find stereo-based approaches in which two calibrated cameras are used to build a 3D map of the environment, which is represented by a set of visual landmarks referred to a common system, being each landmark accompanied by a visual descriptor computed from its visual appearance. Other approaches use a single camera to build a map of the environment. For example in (Civera et al., 2008) a single camera is used to build a 3D map of the environment of visual landmarks extracted with the Harris corner detector (Harris and Stephens, 1988). The camera is moved by hand. When viewed from different viewpoints separated with a sufficient baseline, the 3D position of the landmarks can be estimated. The trajectory of the camera and the position

of the landmarks can be estimated up to a scale factor. The performance of the single-camera SLAM is improved when using a wide field of view lens (Andrew J. Davison et al., 2004), which suggests that using an omni-directional camera would be advantageous in visual SLAM, since the horizontal field of view is maximum.

We consider the case in which a mobile robot is equipped with a single omni-directional camera, as shown in Figure 1(a). Each image is processed to extract interest points that can be matched from different viewpoints. We consider that the robot captures an omnidirectional image. Next, the robot moves and captures a different omnidirectional image. If we assume that a set of significant points can be extracted and matched in both images, the relative movement between the images can be computed (Scaramuzza et al., 2009). In particular, the rotation between images can be univocally computed, as well as the translation (up to a scale factor). To obtain these measurements between images we rely on a modification of the Seven Point Algorithm (Scaramuzza et al., 2009). In Figure 1(b) we present two omnidirectional images, where some correspondences have been indicated. The transformation between both reference systems is shown. In the experiments we rely on the SURF features for the detection and description of the points. In the SLAM infrastructure presented here, the image  $I_0$  will be named a *view*, in order to differentiate from the commonly used visual landmarks. In this sense, a *view* is an image captured from a pose in the environment that is associated with a set of bi-dimensional points extracted from it. It is worth noting that a visual landmark corresponds to a physical point, such as a corner on a wall. However, the *view* represents the visual information that is obtained from a particular pose in the environment.

In this paper we propose a different representation of the environment in the visual SLAM problem. Instead of estimating the position of a set of visual landmarks in the environment we consider the position and orientation of a set of views in the environment. When the robot moves in the neighbourhood of the view and captures an image with the camera, a set of interest points will be matched between the current image and the view, thus allowing to localize the robot with respect to it. When the robot moves away from the image, the appearance of the scene will vary and it may be difficult to find corresponding points. In this case, a new view will be created at the current position of the robot with an uncertainty. The new view will allow the localization of the robot around its neighbourhood. It is worth noting that this representation has been previously used in the context of localization.

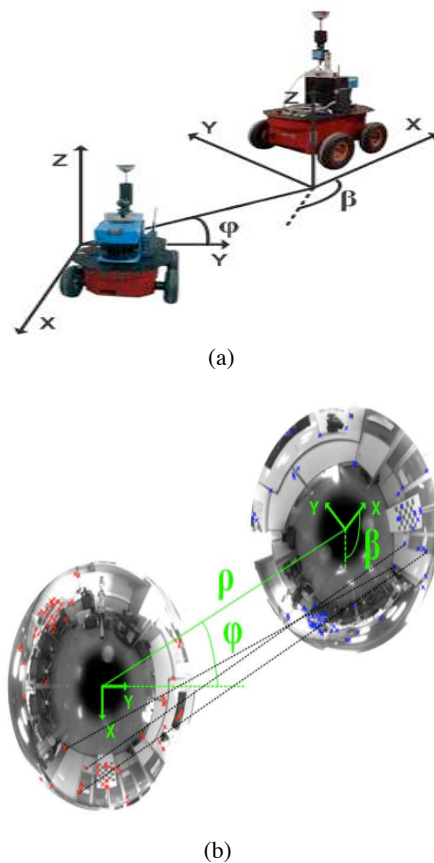


Figure 1: Figure 1(a) shows the sensor setup used during the experiments. Figure 1(b) presents two real omnidirectional images acquired, with some correspondences indicated.

For example, in (Fernandez et al., 2010) a set of omnidirectional images acquired at certain points in the environment are used to localize the environment using a Monte-Carlo algorithm and a global appearance-based comparison of the images. In (Konolige et al., 2010) a view-based map is proposed. Connections between different stereo views are formed by consistent geometric matching of their features. The map is estimated with a graph optimization technique. However, in the approach presented here, an omnidirectional camera is used instead, which allows us to represent the environment with a low number of omnidirectional images. In addition, the transformation between views can only be computed up to a scale factor, thus the restrictions between views cannot be geometric.

The approach proposed in this paper presents some advantages over previous visual SLAM approaches. The most important is the compactness of the representation of the environment. For example, in (Andrew J. Davison et al., 2004; Civera et al., 2008) an Extended Kalman Filter (EKF) is used to estimate

the position of the visual landmarks, as well as the position and orientation of the camera. In (Civera et al., 2008) 6 variables are used to represent each landmark, thus the state vector in the EKF grows rapidly with the number of landmarks in the environment. This fact poses a challenge for most existing SLAM approaches. In opposition with these, in the algorithm presented here, only the pose of a reduced set of views is estimated. Thus, each view encapsulates information of a particular area in the environment, in the form of several interest points detected in the image. Typically, as will be shown in the experiments, a single view may retain a sufficient number of interest points so that the localization in its neighbourhood can be performed.

The main disadvantage of the presented approach, is, nevertheless, the computational cost of determining a metric transformation between two omnidirectional images. However, in Section 4 we present an algorithm that can be used to process images at a fast rate and can be used for online SLAM. In this case, the computation of the transformation between two images depends only on the number of matches, that can be easily adjusted to provide both speed and precise results.

We present a series of results obtained in simulation and with real omnidirectional images that demonstrate the validity of the approach. We first compute a gaussian observation noise model for the measurements between images. Based on this model, we present a series of experiments in a simulated environment. Finally, we present results using real images captured in an office-like environment.

The rest of the paper is organized as follows. First, Section 2 presents some related work in the field of visual SLAM. Next, Section 3 describes the SLAM process in this kind of architecture. The algorithm used to estimate the transformation between two omnidirectional images is described in Section 4. Finally, Section 5 presents experimental results.

## 2 RELATED WORK

We can classify the different visual SLAM approaches with respect to:

- The sensor used, mainly: stereo cameras, a single camera or omnidirectional camera.
- The detection of significant points or regions: that is the method used to extract robust points that can be matched across images. For example the Harris corner detector has been extensively used in the visual SLAM field (Davison and Murray, 2002; Gil et al., 2010b).

- The visual description of the points: the visual landmarks are commonly described in order to be distinguished and associated in the map. The SIFT (Lowe, 2004) and SURF (Bay et al., 2006) have been used extensively in the context of visual SLAM.
- The representation of the map: commonly the map is represented by a set of visual landmarks. Each visual landmark is a point-feature in the environment that can be easily detected in the images. In the map, each landmark is stored as a 3D position along with a visual descriptor, partially invariant to view changes.
- The SLAM algorithm: such as an EKF-based approach, Rao-Blackwellized particle filters, etc.

For example, in (Se et al., 2001) stereo vision is used to extract 3D visual landmarks from the environment. During exploration, the robot extracts SIFT features from stereo images and calculates relative measurements to them. Landmarks are then integrated in the map with a Kalman Filter associated to each one. In (Gil et al., 2006) a Rao-Blackwellized particle filter is used to estimate simultaneously the map and the path of a single robot exploring the environment. A single low-cost camera is used in (Davison and Murray, 2002) to estimate a map of 3D visual landmarks and the 6 DOF trajectory of the camera with an EKF-SLAM algorithm. The interest points are detected with the Harris corner detector (Harris and Stephens, 1988) and described with a grey level patch. Since distance cannot be measured directly with a single camera, the initialization of the XYZ coordinates of a landmark poses a problem. This fact inspired the inverse depth parametrization exposed in (Civera et al., 2008). A variation of the Information Filter is used in (Joly and Rives, 2010) to estimate a visual map using a single omnidirectional camera and an inverse depth parametrization of the landmarks. Finally, in (Jae-Hean and Myung Jin, 2003) two omnidirectional cameras are combined to obtain a wide field of view stereo vision sensor. In (Scaramuzza et al., 2009), the computation of the essential matrix between two views allows to extract the relative motion between two camera poses, which leads to a visual odometry.

## 3 SLAM

In this section we describe in detail the representation of the environment as well as the creation of the map. The visual SLAM problem is solved in a dual manner. Instead of estimating the position of a set of



visual landmarks, we propose the estimation of the position and orientation of a set of views obtained from the environment. Thus, the map is formed by a set of omnidirectional images obtained from different positions in the environment. In opposition with other solutions, the landmarks do not correspond to any physical element in the environment (e.g. a corner, or the trunk of a tree). In our case, a landmark (renamed *view*) will be constituted by an omnidirectional image captured at the pose  $x_l = (x_l, y_l, \theta_l)$  and a set of interest points extracted from that image.

In our opinion, the SLAM architecture presented in this paper is suitable for different kind of SLAM algorithms, online methods such as, EKF, FastSLAM or offline, such as, for example, Stochastic Gradient Descent (Grisetti et al., 2007). In this paper we present the application of the EKF to the map representation proposed and show how to obtain correct results using real data.

In addition we consider that the map representation and the measurement model can be also be applied using standard cameras. The reason for using omnidirectional images is their ability to acquire a global view of the environment in a single image.

### 3.1 Map Representation

We propose the estimation of the pose  $x_v = (x_v, y_v, \theta_v)^T$  of a mobile robot at each time  $t$  as well as the pose of  $N$  views. Each view  $i$  is constituted by its pose  $x_{l_i} = (x_{l_i}, y_{l_i}, \theta_{l_i})^T$ , its uncertainty  $P_{l_i}$  and a set of  $M$  interest points  $p_j$  expressed in image coordinates. Each point is associated with a visual descriptor  $d_j$ ,  $j = 1, \dots, M$ .

This map representation is shown in Figure 2, where the position of several views is indicated. For example, the view  $A$  is stored with a particular pose  $x_{l_A} = (x_{l_A}, y_{l_A}, \theta_{l_A})^T$  in the map and has a set of  $M$  points detected in it. The view  $A$  allows the localization of the robot in the corridor. The view  $B$  represents the first room, whereas the view  $C$  represents a second room 2, and allows the robot to localize in it.

The augmented state vector is thus defined as:

$$x = \begin{bmatrix} x_v \\ x_{l_1} \\ x_{l_2} \\ \dots \\ x_{l_N} \end{bmatrix} \quad (1)$$

where  $N$  is the number of views that exist in the map.

### 3.2 Map Building Process

We present an example of map building in an office-like indoor environment, also described in Figure 2.

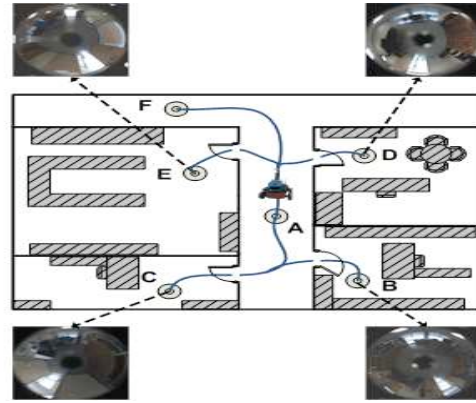


Figure 2: The figure presents the basic idea in map creation. The robot starts the exploration from the point  $A$  and stores a view  $I_A$  at the origin. Next, the robot moves. When no matches are found between the current image and  $I_A$ , a new view is created at the current position of the robot  $B$ . The process continues until the whole environment is represented

We consider that the robot starts the exploration at the origin denoted as  $A$ , placed at the corridor. At this point, the robot captures an omnidirectional image  $I_A$ , that will be used as a *view*. We assume that, when the robot moves inside the corridor, several correspondences can be found between  $I_A$  and the current omni-directional image. When the robot enters the first room, the appearance of the images vary significantly, thus, no matches are found between the current image and image  $I_A$ . In this case, the robot will initiate a new *view* named  $I_B$  at the current robot position. Finally, the robot goes into a different room and creates a new *view* named  $I_C$ .

### 3.3 Observation Model

In the following we describe the observation model proposed. We assume that there exist two omnidirectional images obtained from two different poses in the environment. One of the images is stored in the map and the other is the current image captured by the robot. We assume that given two images we are able to extract a set of significant points in both images and obtain a set of correspondences. Next, as will be described in Section 4, we are able to obtain the observation  $z_t$ :

$$z_t = \begin{pmatrix} \phi \\ \beta \end{pmatrix} = \begin{pmatrix} \arctan\left(\frac{y_{l_n} - y_v}{x_{l_n} - x_v}\right) - \theta_v \\ \theta_{l_n} - \theta_v \end{pmatrix} \quad (2)$$

where the angle  $\phi$  is the bearing at which the view  $n$  is observed and  $\beta$  is the relative orientation between the images. The landmark  $n$  is represented by

$x_{l_n} = (x_{l_n}, y_{l_n}, \theta_{l_n})$ , whereas the pose of the robot is described as  $x_v = (x_v, y_v, \theta_v)$ . Both measurements  $(\phi, \beta)$  are represented in Figure 1(a).

### 3.4 New View Initialization

A new omnidirectional image is included in the map when the number of matches found in the neighbouring views is low. In particular, we use the following ratio:

$$R = \frac{2m}{n_A + n_B} \quad (3)$$

that computes the similarity between views  $A$  and  $B$ , being  $m$  the total number of matches between  $A$  and  $B$  and  $n_A$  and  $n_B$  the number of detected points in images  $A$  and  $B$  respectively. The robot decides to include a new view in the map whenever the ratio  $R$  drops below a pre-defined threshold. In order to initialize a new view, the pose of the view is obtained from the current estimation of the robot pose. The uncertainty in the pose of the landmark equals in this case the uncertainty in the pose of the robot.

### 3.5 Data Association

The data association problem in a feature-based SLAM algorithm can be posed in the following way: given a set of observations  $z_t = \{z_{t,1}, z_{t,2}, \dots, z_{t,B}\}$  obtained at time  $t$ , compute the landmarks in the map that generated those observations. Thus, the result of the data association is a vector of  $B$  indexes  $H = \{j_1, j_2, \dots, j_B\}$ , where each index  $j_i \in [1, N+1]$  denotes one of the landmarks in the map, being  $N$  the total number of landmarks. If the observation  $z_{t,i}$  does not correspond to any of the landmarks in the map, a new one is initialized with index  $N+1$ . Finding the correct data associations is crucial in SLAM, since false data associations may cause the SLAM filter to diverge. Finding the correct data association can be complex if the landmarks are close together and this fact has inspired solutions such as the Joint Compatibility Test (Neira and Tardós, 2001). In the approach presented here the data association process can be tackled in a more simple way. Consider, for example, that at time  $t$  the robot captures an omnidirectional image  $I_t$  and extracts a set of interest points. To find the data association, we proceed in the following way: First, we select a subset of candidate views from the map. The selection is based on the Euclidean distance:

$$D_i = \sqrt{(x_v - x_{l_i})^T \cdot (x_v - x_{l_i})}. \quad (4)$$

The view  $i$  is included in the candidate set if  $D_i < \delta$ , where  $\delta$  is a pre-defined threshold. Higher values of  $\delta$

allow the loop closure with a higher accumulated error in the pose, but need a higher computational cost. Next, we look for a set of matching points between the current image  $I_t$  and each of the images in the candidate set  $\{I_1, I_2, \dots, I_J\}$ . We can compute an observation  $z_t = (\phi, \beta)$  to any of the images in the candidate set if the number of matches is sufficient. As will be explained in Section 4 we are able to compute an observation with only 4 matches. However, in practice, we require a higher number of matches in order to reject false correspondences. In addition, we compute the ratio  $R$  defined in Equation 3 and initialize a new view whenever this ratio goes below 0.5.

## 4 TRANSFORMATION BETWEEN OMNI-DIRECTIONAL IMAGES

In this section we present a method to obtain the relative angles  $\beta$  and  $\phi$  between two omni-directional images, as represented in Figure 1(b). These angles reveal the relative pose of the robot and allow for its localization. This poses the problem of detecting feature points in both images and finding the correspondences between images in order to recover a certain camera rotation and translation by applying epipolar constraints. Traditional schemes, such as (Kawanishi et al., 2008; Nister, 2003; Stewenius et al., 2006) solve the problem in the general 6 DOF case, whereas in our case, according to the specific motion of the robot on a plane, we are able to reduce it to 4 variables, thus the resolution is simplified in terms of computational cost. The obtention of the relative angles between two poses of the robot takes approximately  $t = 0.4msec$ , which confirms the capability to work in real-time.

### 4.1 Significant Point Detection and Matching

We are using SURF features (Bay et al., 2006) in order to find interest points in the images. According to (Gil et al., 2010a), SURF features are able to outperform other detectors and descriptors in terms of robustness of the detected points and invariance of the descriptor. Moreover in (Murillo et al., 2007) SURF points detection succeed with omnidirectional images. We transform the omnidirectional images into a panoramic view in order to increase the number of valid matches between images due to the lower appearance variation obtained with this view. The method to obtain robust correspondences of SURF points across images has been based on keypoint

matching ratios reported in (Lowe, 2004). Then, the process is inverted to recover the coordinates into the original omnidirectional view.

## 4.2 Computing the Transformation

Once SURF points are detected and matched in two images it appears the necessity to establish a process to retrieve relative angles  $\beta$  and  $\phi$ .

### 4.2.1 Epipolar Geometry

The epipolar condition establishes the relationship between two 3D points seen from different views.

$$p'^T E p = 0 \quad (5)$$

where the matrix  $E$  is denoted as the essential matrix and can be computed from a set of corresponding points in two images. The same point detected in two images can be expressed as  $p = [x, y, z]^T$  in the first camera reference system and  $p' = [x', y', z']^T$  in the second camera reference system. In our case, since only one camera is employed, images are taken from two unknown poses without knowledge about the distance between them. This fact leads to a lack of depth information, and the solution can only be recovered up to a scale factor  $\rho$ . In addition, essential matrix  $E$ , represents a specific rotation  $R$  and a translation  $T$  (up to a scale factor) between the two image reference systems, with  $E = R \cdot T_x$ . Thus the desired angles can be recovered from the decomposition of  $E$ . Please note that Epipolar Geometry can be used with omnidirectional images since we back-project 2D image-plane system to 3D using a modelled hyperbolic camera's mirror, which is provided by means of a previous calibration step (Scaramuzza et al., 2006). Because of the depth ambiguity, we denote  $\vec{p}$  and  $\vec{p}'$  in 3D, as the unitary vectors that indicate the direction of the points in the two reference systems, since the 3D position cannot be completely defined with only one view of the scene.

To accomplish the objective of obtaining  $\beta$  and  $\phi$ , we have considered the approach (Hartley and Zisserman, 2004) which suggests retrieving directly the projection matrix  $P$ , that also defines the transformation between images. This method has been adopted, since it provides a simple way to compute the four possible solutions to the problem. First, we apply the epipolarity constrain  $\vec{p}'^T \cdot E \cdot \vec{p} = 0$  to  $N$  points, and solve the resulting Equation  $D \cdot E = 0$ . Next we apply SVD decomposition to  $E$ :

$$[U|S|V] = SVD(E) \quad (6)$$

that allows to compute:

$$R_1 = [UV^T W] \quad (7)$$

$$R_2 = [UV^T W^T] \quad (8)$$

$$T = [UZU^T] \quad (9)$$

being  $W$  and  $Z$  auxiliary matrices (Hartley and Zisserman, 2004) and both possible rotations ( $R_1, R_2$ ) and translations ( $T_{1x}, -T_{1x}$ ). To obtain the four possible P-matrices, we compute:

$$\begin{aligned} P_1 &= [R_1 | T_{1x}], P_2 = [R_1 | -T_{1x}], \\ P_3 &= [R_2 | T_{1x}], P_4 = [R_2 | -T_{1x}], \end{aligned} \quad (10)$$

In our case, the projection matrices have the following form:

$$P_i = \begin{bmatrix} \cos(\beta) & -\sin(\beta) & 0 & \rho \cos(\phi) \\ \sin(\beta) & \cos(\beta) & 0 & \rho \sin(\phi) \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (11)$$

Notice that  $\beta$ ,  $\phi$  and  $\rho$  may take different values that satisfy the epipolar condition (5) due to the undetermined scale factor  $\rho$ . This poses the problem of selecting one of the four possible solutions described in Equation (10), which will be detailed in the following subsection.

### 4.2.2 Selecting a Solution

In order to find the correct solution, an inverse procedure has to be carried out. We multiply  $\vec{p}'$  by the inverse of the four projection matrixes  $P_i$ , obtaining four estimations of  $\vec{p}$ . The less deviated one respect to  $\vec{p}$  is assumed to have been obtained through the correct solution. Finally,  $\beta$  and  $\phi$  are directly recovered from the elements of  $P$  as defined in Equation (11).

Since we are estimating a rotation and a translation of a planar motion on the XY plane, only  $N = 4$  correspondences suffice to solve the problem. It is easy to show that the matrix  $E$  has only 4 non-zero elements. However, in order to obtain a better solution in the presence of noise and false correspondences, we process more points in the computation and use RANSAC for outlier rejection (Nistér, 2005). In particular, it is worth noticing that the SURF features can be tuned to obtain a reduced set of highly robust points. In consequence, we obtain a reduced set of matches, thus leading to a fast computational time.

## 5 RESULTS

We present three different experimental sets. First, in Section 5.1 we present results obtained in simulation that validate the SLAM approach proposed here.

Next, Section 5.2 presents the results using real data captured with a Pioneer P3-AT indoor robot. The robot is equipped with a firewire 1280x960 camera and a hyperbolic mirror. The optical axis of the camera is installed approximately perpendicular to the ground plane, as described in Figure 1(a), in consequence, a rotation of the robot corresponds to a rotation of the image with respect to its central point. In addition, we used a SICK LMS range finder in order to compute a ground truth using the method presented in (Stachniss et al., 2004).

### 5.1 SLAM Results in Simulation

We performed a series of experiments in simulation in order to test the suitability of the proposed SLAM scheme. Please note the importance of assuring the convergence of an EKF-based SLAM algorithm when a new observation model is introduced. Figure 3(a) presents the simulation environment 1. The true path followed by the robot is shown with continuous line, whereas the odometry is represented in dashed line. A set of views have been placed randomly along the trajectory and shown with a dot. Please note that the placement of the views depends of the appearance of the images and the ratio  $R$  selected. In the simulation we have placed the views randomly with distances similar to the real case.

The robot starts the SLAM process at the origin and performs two turns along the trajectory. The range, i.e. the capability of computing the observation  $z_t = (\phi, \beta)^T$  at a given distance is shown with a dash-dotted line. The observations obtained by the robot have been simulated using the observation model presented in Equation 2 with an added gaussian noise with  $\sigma_\phi = \sigma_\beta = 0.1 \text{ rad}$ . Figure 3(b) presents the simulation environment 2, which emulates a typical indoor environment, where the computation of the observations is restricted by the walls. We performed a series of experiments when varying the range of the observed views. The results are presented in Figure 4(a) and 4(b), where we present the RMS error in the trajectory when the range of the sensor is varied. We compare the EKF solution (continuous line) to the odometry (dashed line) when compared to the laser-based ground-truth. We generated different odometry sets randomly and repeated the experiment 50 times. In Figure 4(a) we present the mean and  $2\sigma$  intervals. As can be observed in Figure 4(a) when the range is  $0.5m$  the uncertainty in the pose grows without bound and the filter is not able to converge. It can be observed that the RMS error decreases when the sensor range goes beyond  $3m$ . A similar result is presented in Figure 4(b), which corresponds to the simulation

environment 2. In this case, nice results are obtained when the range is over  $9m$ , since the walls restrict the visibility of the *views* and makes the convergence of the filter more difficult. Please note that the results depend strongly on the placement of the *views*, placing more views allows to compute a more precise map and trajectory, however it requires a higher computational cost.

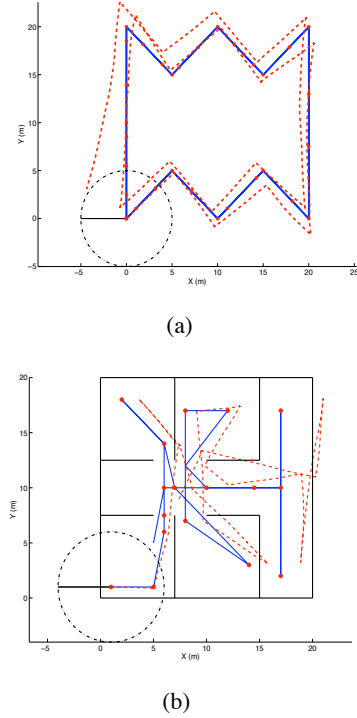


Figure 3: Figure 3(a) represents the simulation environment 1. The location of the different views in the map is represented by dots. Figure 3(b) presents the simulation environment 2.

### 5.2 SLAM with Real Data

In this section we present SLAM results that validate the approach presented here. The robot is guided through the environment and captures omnidirectional images along the trajectory and laser range data. Again, in order to compare the results, we use a laser-based SLAM algorithm, as described in (Stachniss et al., 2004). The robot starts by initializing an omnidirectional image at the origin, as indicated in Figure 5(a). Next, it starts to move along the trajectory while capturing omnidirectional images. A new view is initialized a few steps later, as indicated in Figure 5(a) with an error ellipse. While mapping, the current image is compared with the rest of the views in the map, and a set of correspondences is found. In

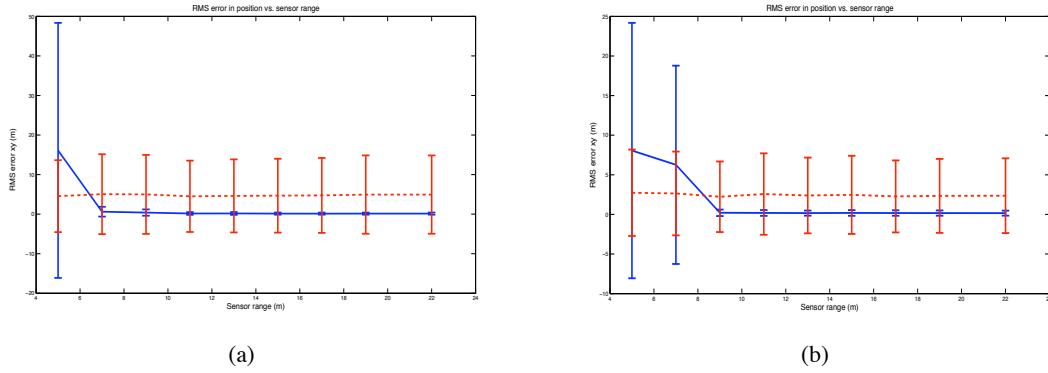


Figure 4: Figure 4(a) presents the results obtained in the simulation environment 1. Figure 4(b) presents the results obtained in the simulation environment 2.

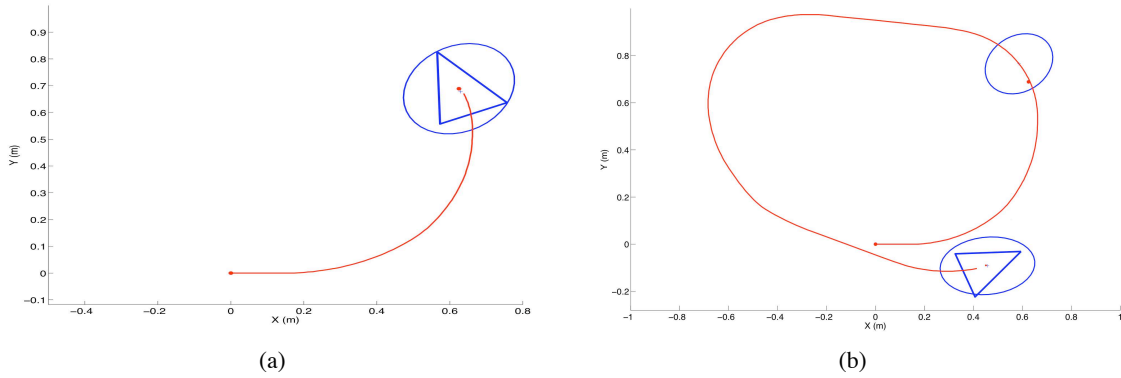


Figure 5: Figure 5(a) and 5(b) present two initial steps in the creation of the map shown in Figure 6.

addition, the similarity ratio (3) is computed. Whenever the similarity of the current image drops below  $\delta_R = 0.5$  a new *view* is created and initialized at the current robot position. In Figure 5(b) we present the occurrence of this event, where a third view is initialized. Finally, the robot performs the trajectory shown in Figure 6(a), where we show with dots the rest of the poses where the robot decided to initialize a new image. We present with a dashed line the ground truth, whereas the EKF estimation is drawn with continuous line. The odometry is represented with a dash-dotted line. It is worth noting that the robot continues to move inside the same room and is able to compute observations of the views initialized before. In our case, the threshold  $\delta_R$  was selected experimentally in order to have a reduced set of views that represent the environment in a compact manner. If a lower  $\delta_R$  is selected, less images are initialized in the map. On the contrary, if a greater value of  $\delta_R$  is selected (i.e. 0.9), the final map will have a large number of views. As can be seen in Figure 6(a) once the fourth view is initialized, no more views are initialized, thus leading to a compact representation of this environment. In

Figure 6(b) we compare the estimated trajectory with the ground truth and the odometry at every step of the trajectory. We present the error in the estimated trajectory (dashed line) with  $2\sigma$  interval and the error in the odometry (dash-dotted line).

Figure 7 presents another experiment. In this case, the robot explores a room, travels through a corridor, goes into a different room and returns. The total traversed distance is 45m. Figure 7(a) presents the ground-truth trajectory (dashed line), the odometry (dash-dotted line) and the estimation (continuous line). The location of the views and its associated uncertainty is indicated with error ellipses. On Figure 7(b) we present the error in the pose at every step of the SLAM process with  $2\sigma$  intervals.

## 6 CONCLUSIONS

We have presented an approach to the Simultaneous Localization and Mapping (SLAM) problem using a single omnidirectional camera. We propose a different representation of the environment. Instead of es-

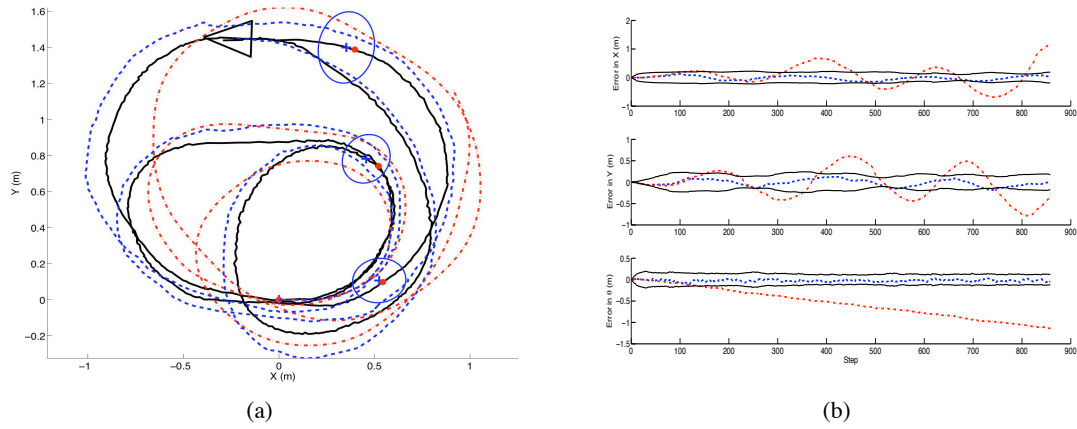


Figure 6: Figure 6(a) presents the results of SLAM using real data with ground-truth (dashed), estimation (continuous) and the odometry (dash-dotted). The position of the views is presented with error ellipses. Figure 6(b) presents the error in  $X$ ,  $Y$  and  $\theta$  at each time step of the estimation (dashed) and the odometry (dash-dotted).

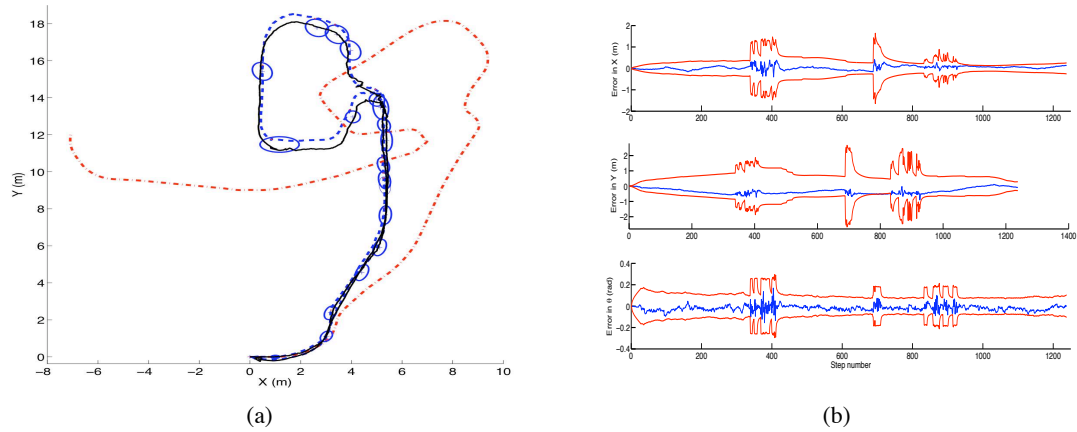


Figure 7: Figure 7(a) presents the results of SLAM using real data with ground-truth (dashed), estimation (continuous) and the odometry (dash-dotted). The position of the views is presented with error ellipses. Figure 7(b) presents the error in  $X$ ,  $Y$  and  $\theta$  at each time step of the estimation (dashed) with a  $2\sigma$  interval.

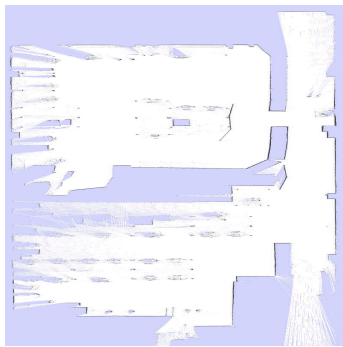


Figure 8: The figure presents the occupancy grid map created during the experiment shown in Figure 7.

timating the 3D position of a set of visual landmarks in the environment, we only estimate the position and

orientation of a set of omnidirectional images. Each omnidirectional image has a set of interest points and visual descriptors associated to it and describes in a compact way the environment. Each omnidirectional image allows the localization of the robot around its neighbouring. Given two omnidirectional images and a set of corresponding points, we are able to compute the rotation and translation (up to a scale factor) between the images. This allows us to propose an observation model and compute a map and a trajectory. We present localization and SLAM results using an EKF-based SLAM algorithm, however, we consider that different SLAM strategies may be used. We present results obtained in a simulated environment that validate the SLAM approach. In addition, we have shown the validity of the approach by using real data captured with a mobile robot.

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